

基于MATLAB的

象棋棋盘及棋子识别

张凌霄 邱子濛 郑睦炜

According to the real-time board photo taken (e.g. Test.png), and the previously known standard chess board(e.g. Ref.png), automatic positioning and output coordinates of all the pieces of both the red side and the black side.

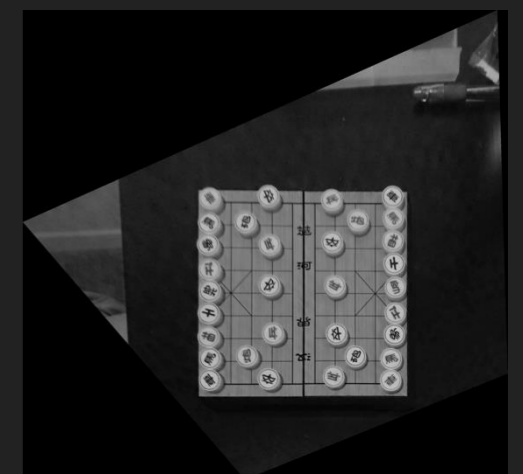
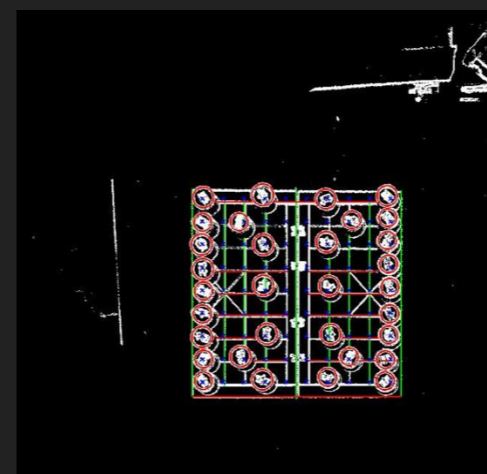
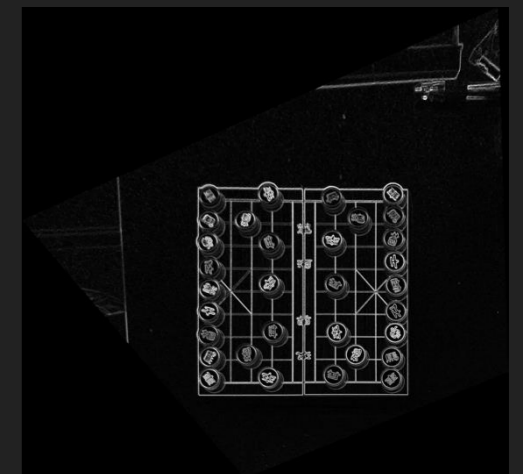
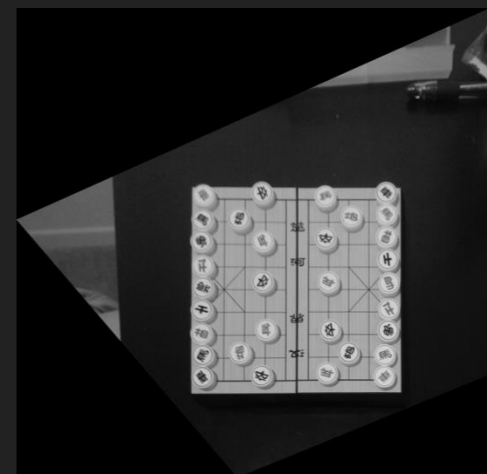
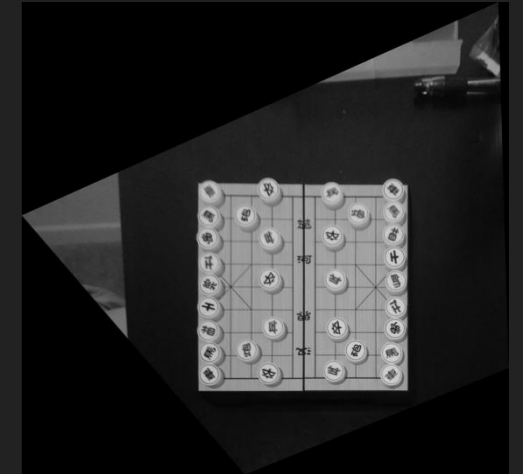
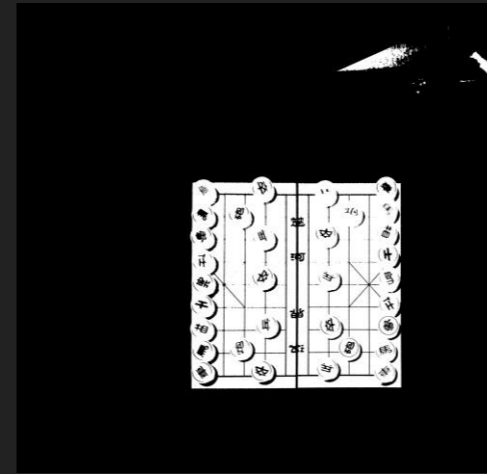
Input: 2 pics

Output: 2 sets of coordinates

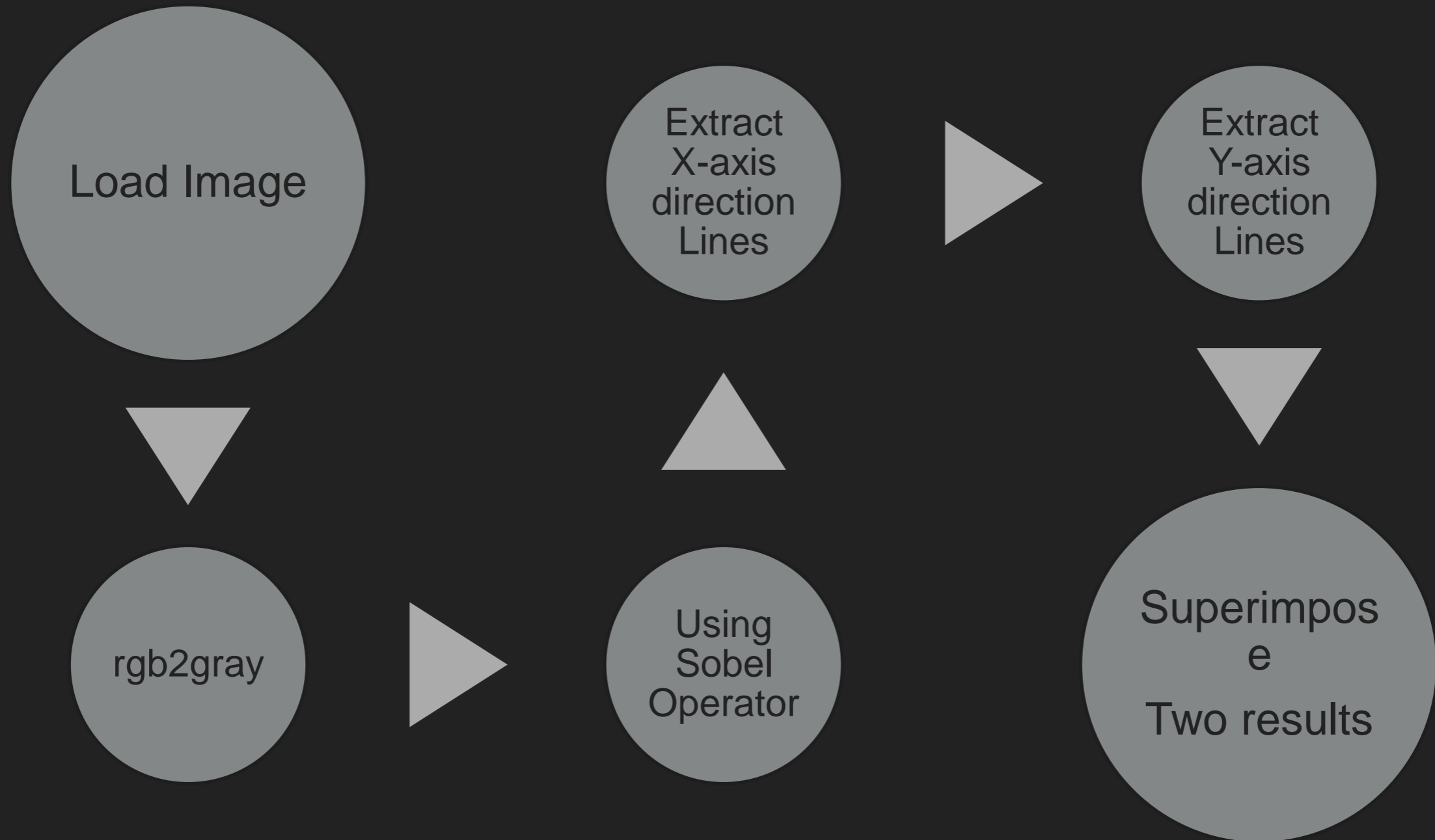
Demand of project

PROCESSING STEPS

- ▶ Edge Detection
- ▶ Perspective Transformation
- ▶ Image Quality Optimize
- ▶ Line detection
- ▶ Position Chess Pieces
- ▶ Identify Pieces' color
- ▶ Identify Pieces' Character



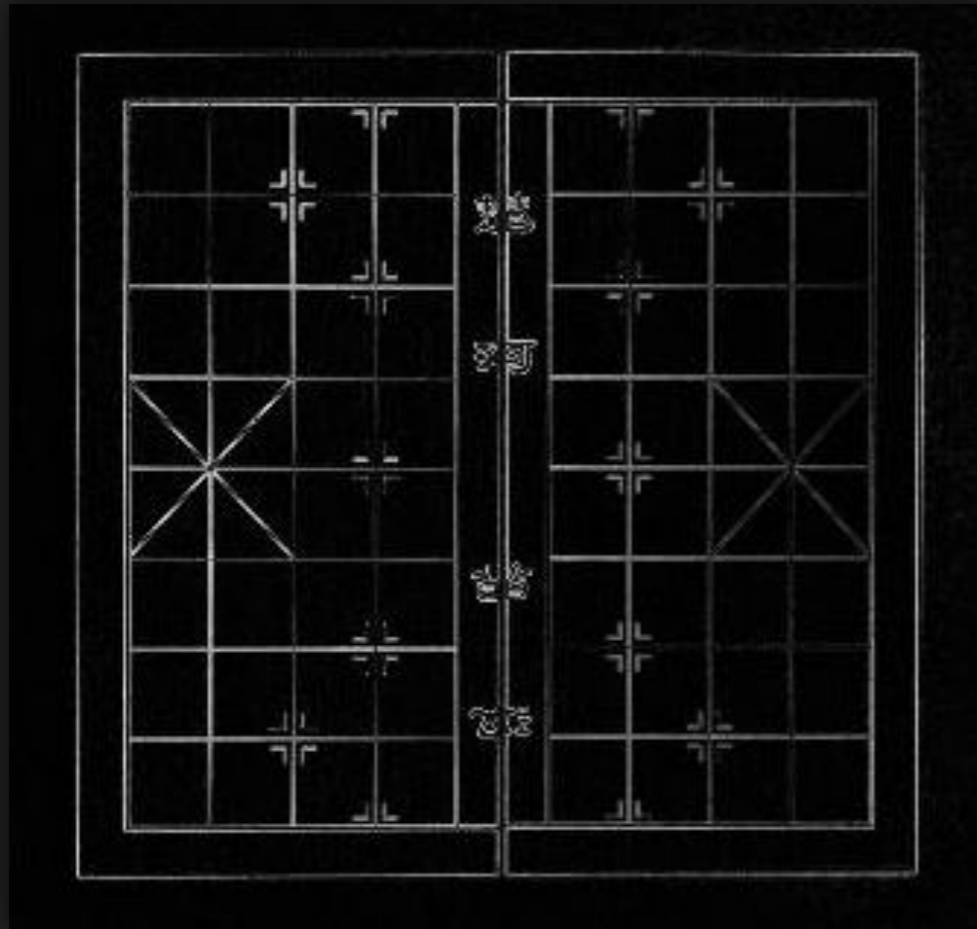
STEP.1 EDGE DETECTION



`sobelKernelY = [1 2 1; 0 0 0; -1 -2 -1]`

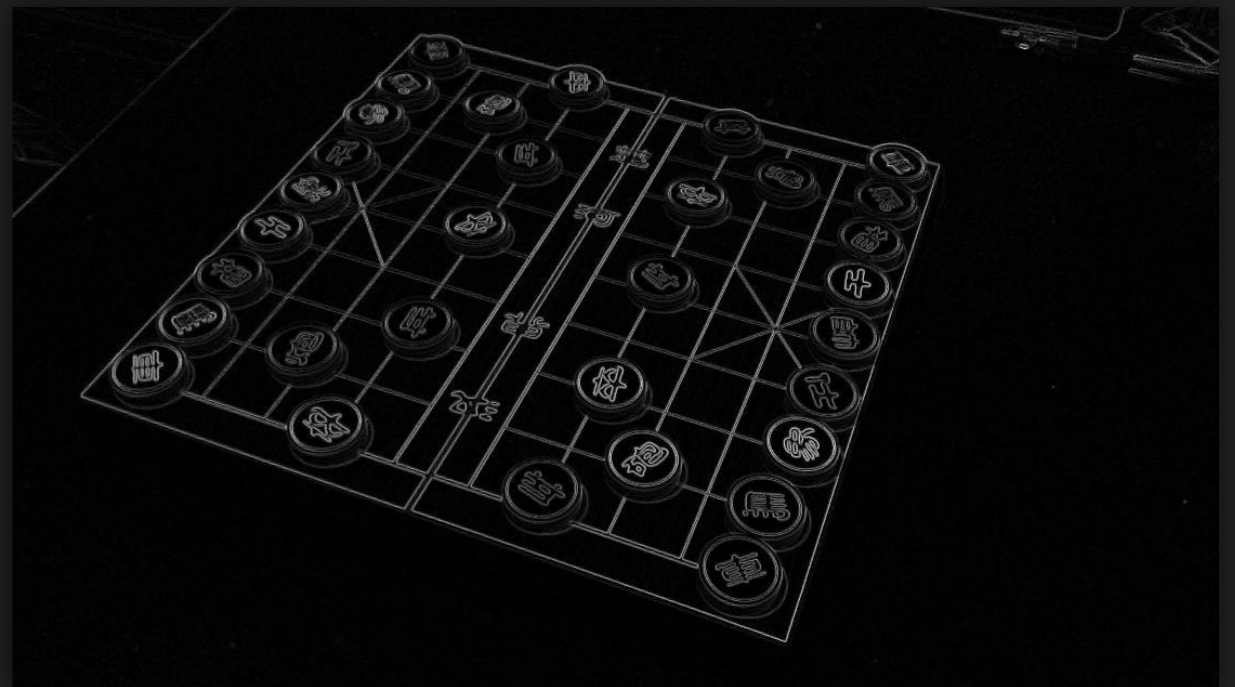
`sobelKernelX = [-1 0 1; -2 0 2; -1 0 1]`

STEP.1 EDGE DETECTION



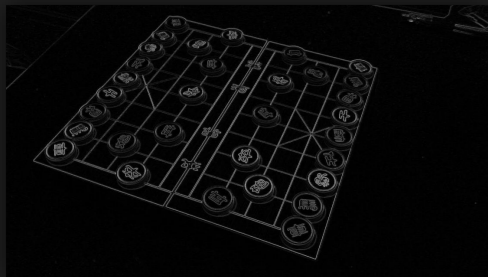
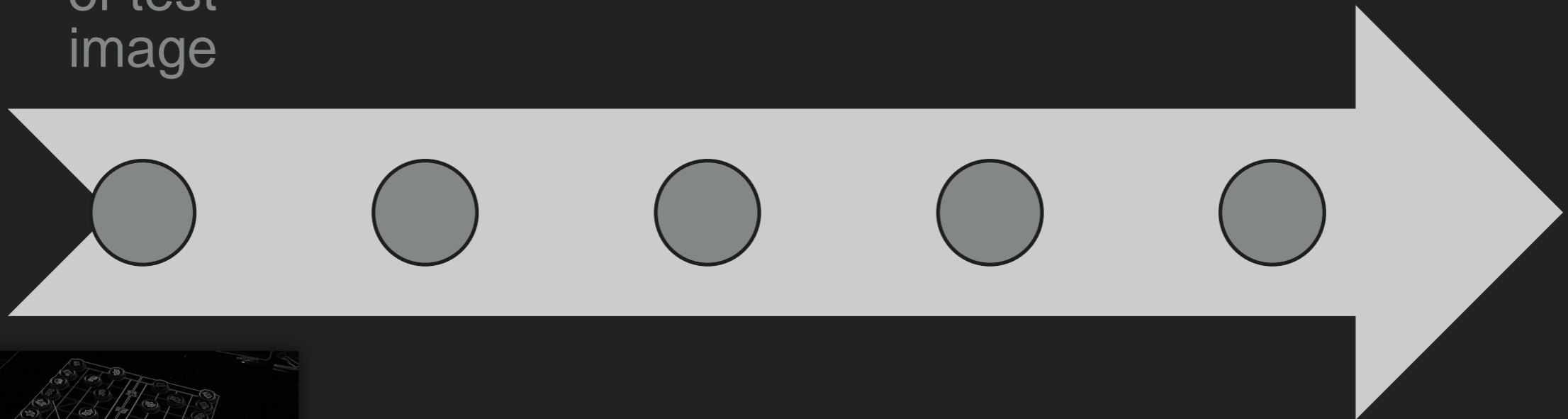
Reference
chess board

Test input
chess board

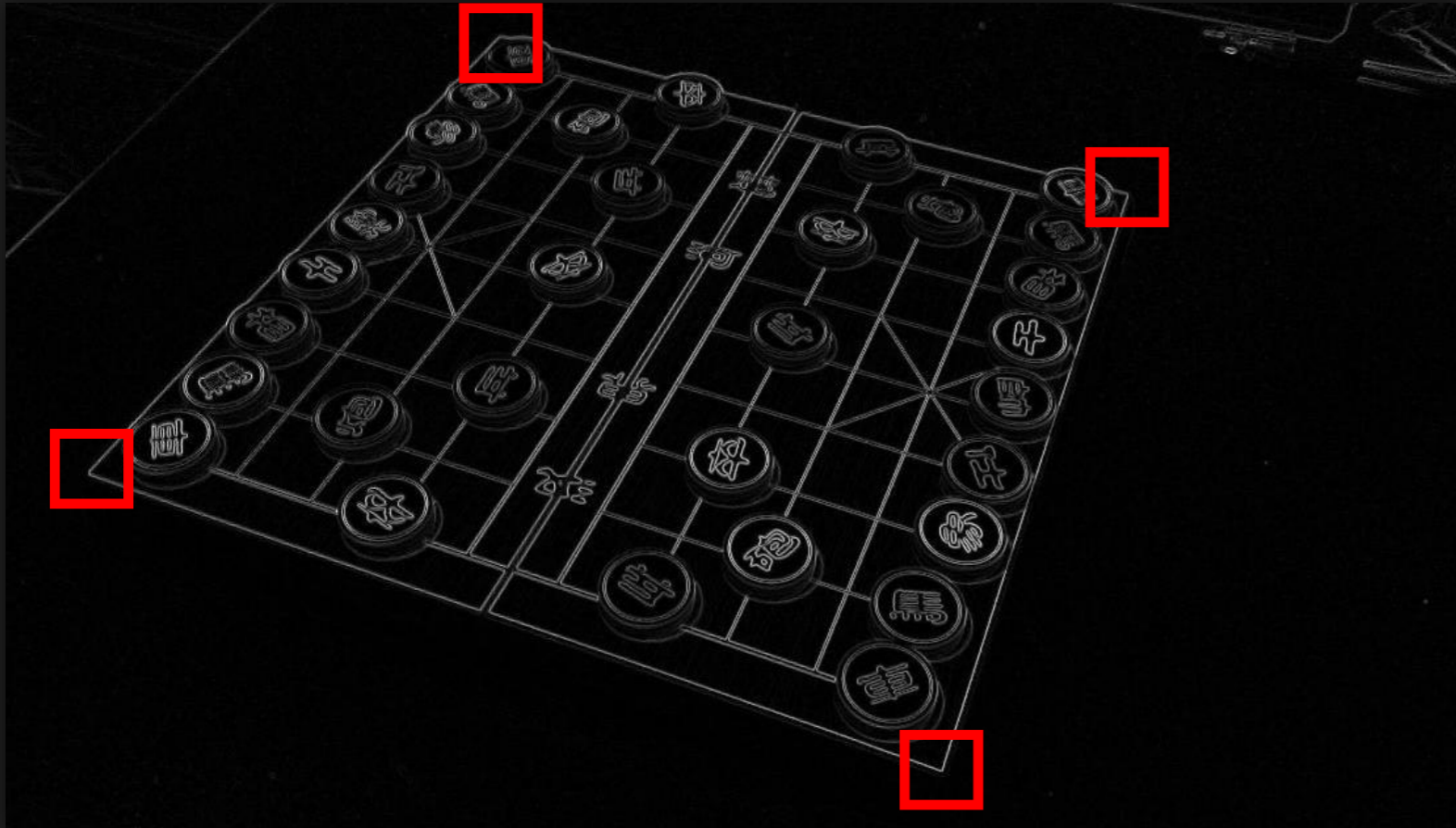


STEP.2 PERSPECTIVE TRANSFORMATION

Auto-locate
the 4
corners
of test
image



STEP.2 PERSPECTIVE TRANSFORMATION



Line Detection



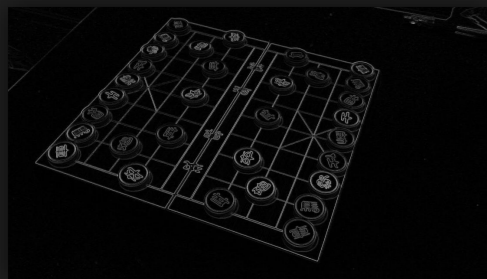
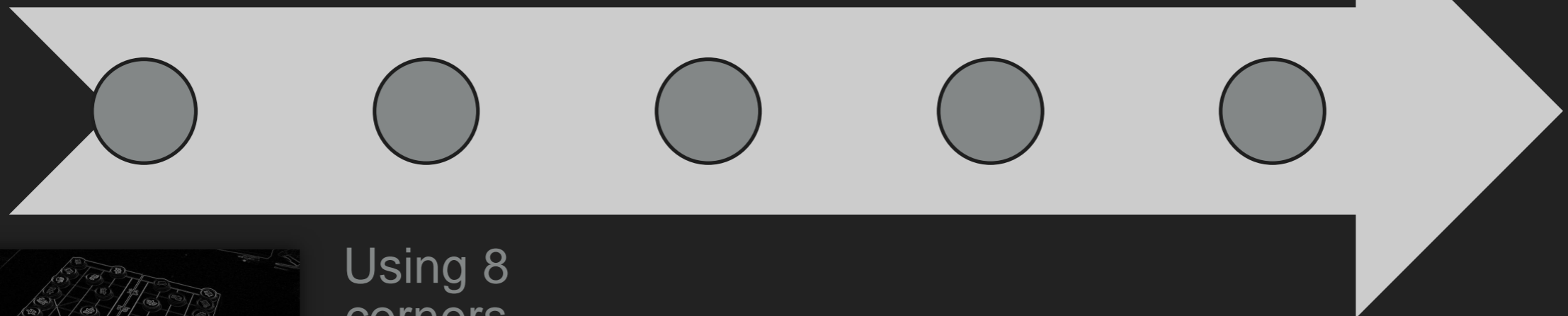
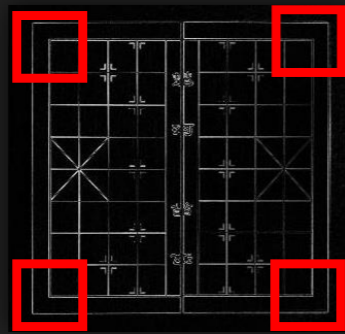
Find the top 4
longest lines



Their
endpoints are
4 corners of
board

STEP.2 PERSPECTIVE TRANSFORMATION

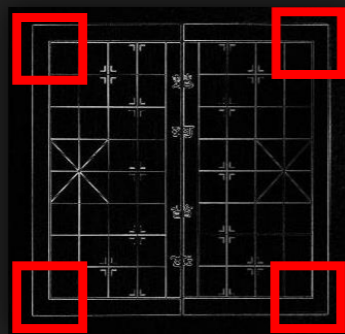
Auto-locate the 4 corners of test image



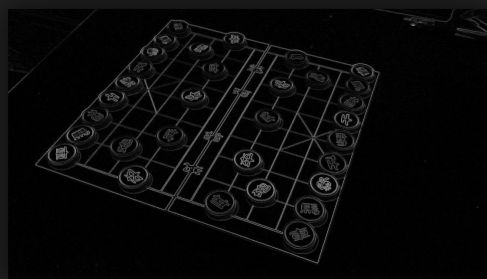
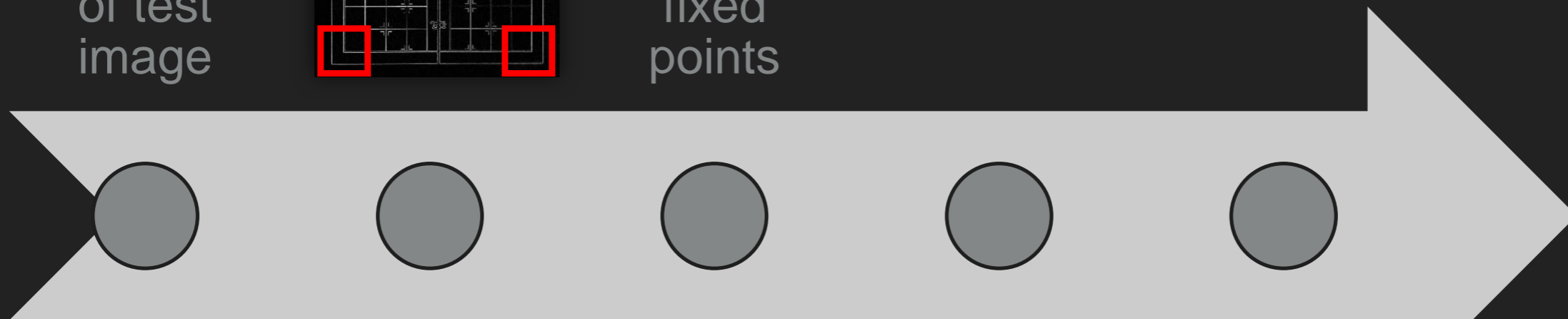
Using 8 corners from Ref and Test image as fixed points

STEP.2 PERSPECTIVE TRANSFORMATION

Auto-locate the 4 corners of test image



Calculate transform matrix with the 8 fixed points



Using 8 corners from Ref and Test image as fixed points

| | | | | | | | | | |
|----|----|----|----|-----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | | | | | |
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| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 11 |
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| 34 | 63 | 84 | 85 | 86 | 87 | 88 | 71 | 46 | 13 |
| 33 | 62 | 83 | 96 | 97 | 98 | 89 | 72 | 47 | 14 |
| 32 | 61 | 82 | 95 | 100 | 99 | 90 | 73 | 48 | 15 |
| 31 | 60 | 81 | 94 | 93 | 92 | 91 | 74 | 49 | 16 |
| 30 | 59 | 80 | 79 | 78 | 77 | 76 | 75 | 50 | 17 |
| 29 | 58 | 57 | 56 | 55 | 54 | 53 | 52 | 51 | 18 |
| 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 |

STEP.2 PERSPECTIVE TRANSFORMATION

$$(x' \ y' \ w') = (u \ v \ w) \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix}$$

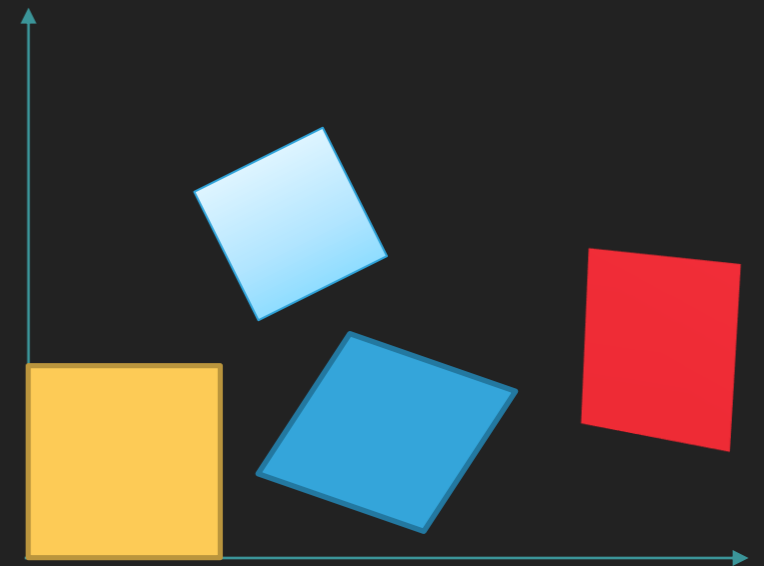
(u, v) refers to the original coordinate, and (x, y) refers to the transformed coordinate.

Where $x = \frac{x'}{w'}$, $y = \frac{y'}{w'}$.

We can split this transform matrix

$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix}$ into 4 parts:

$\begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}$ denotes the linear transform, e.g. scaling, shearing and rotation.



STEP.2 PERSPECTIVE TRANSFORMATION

$$(x' \ y' \ w') = (u \ v \ w) \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix}$$

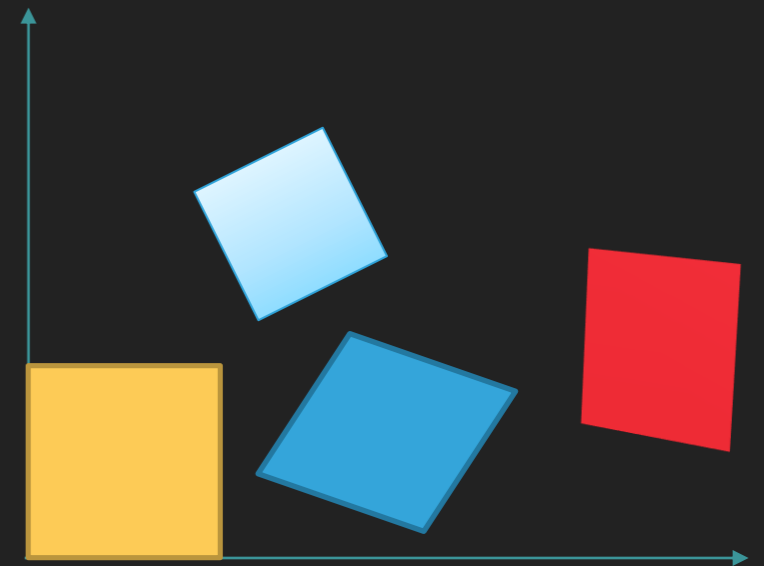
$(a_{31} \ a_{32})$ is applied for translation.

$(a_{13} \ a_{23})^T$ is applied for affine transform.

Then we can obtain,

$$x = \frac{x'}{w'} = \frac{a_{11}u + a_{21}v + a_{31}}{a_{13}u + a_{23}v + a_{33}}$$
$$y = \frac{y'}{w'} = \frac{a_{12}u + a_{22}v + a_{32}}{a_{13}u + a_{23}v + a_{33}}$$

Also if we know the original and transformed coordinates, it is easy to calculate the transform matrix.



STEP.2 PERSPECTIVE TRANSFORMATION

Assuming the coordinates before and after the transformation like

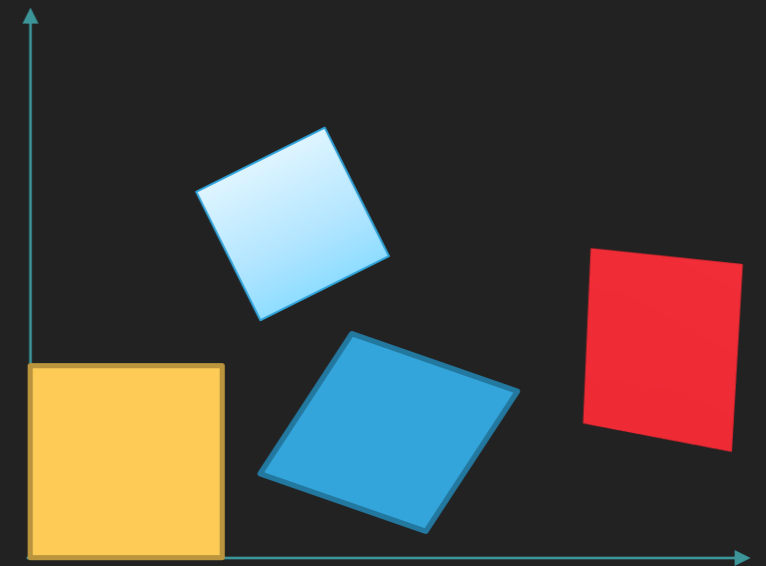
$$\begin{aligned} & (CornerRefX_1, CornerRefY_1) \\ \rightarrow & (CornerTestX_1, CornerTestY_1) \end{aligned}$$

...

$$\begin{aligned} & (CornerRefX_4, CornerRefY_4) \\ \rightarrow & (CornerTestX_4, CornerTestY_4) \end{aligned}$$

According to transform formula, we have

$$\begin{aligned} & a_{31} = x_1 \\ & a_{11} + a_{31} - a_{13}x_2 = x_2 \\ a_{11} + a_{21} + a_{31} - a_{13}x_3 - a_{23}x_3 &= x_3 \\ & a_{12} + a_{31} - a_{23}x_4 = x_4 \\ & \dots \\ & a_{22} + a_{32} - a_{23}y_4 = y_4 \end{aligned}$$



STEP.2 PERSPECTIVE TRANSFORMATION

Therefore,

$$a_{11} = x_2 - x_1 + a_{12}x_2 \quad a_{12} = y_2 - y_1 + a_{13}y_2$$

$$a_{21} = x_4 - x_1 + a_{12}x_3 \quad a_{22} = y_4 - y_1 + a_{13}y_3$$

$$a_{31} = x_0 \quad a_{32} = y_0$$

$$a_{12} = \frac{\begin{vmatrix} \Delta x_1 & \Delta x_3 \\ \Delta y_1 & \Delta y_3 \end{vmatrix}}{\begin{vmatrix} \Delta x_1 & \Delta x_2 \\ \Delta y_1 & \Delta y_2 \end{vmatrix}}$$
$$a_{13} = \frac{\begin{vmatrix} \Delta x_3 & \Delta x_2 \\ \Delta y_3 & \Delta y_2 \end{vmatrix}}{\begin{vmatrix} \Delta x_1 & \Delta x_2 \\ \Delta y_1 & \Delta y_2 \end{vmatrix}}$$

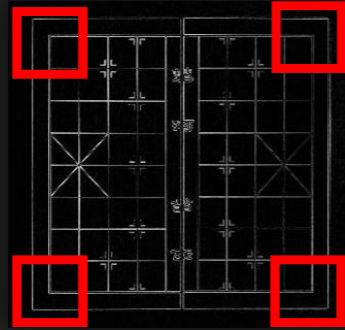
Where,

$$\Delta x_1 = x_2 - x_3 \quad \Delta x_2 = x_4 - x_3 \quad \Delta x_3 = x_1 - x_2 + x_3 - x_4$$

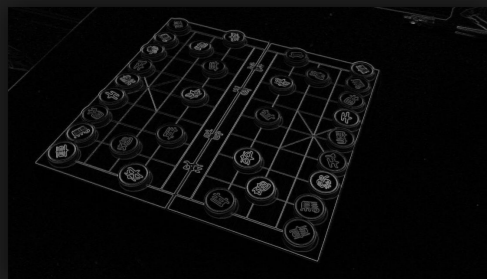
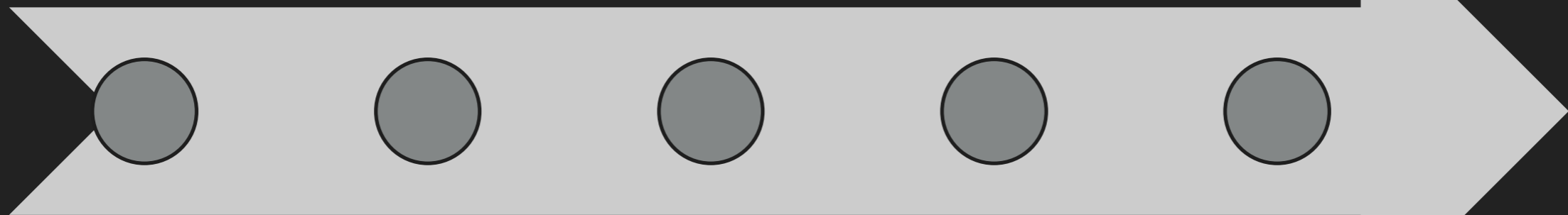
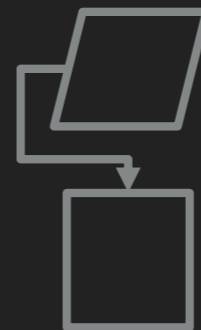
$$\Delta y_1 = y_2 - y_3 \quad \Delta y_2 = y_4 - y_3 \quad \Delta y_3 = y_1 - y_2 + y_3 - y_4$$

STEP.2 PERSPECTIVE TRANSFORMATION

Auto-locate the 4 corners of test image



Calculate transform matrix with the 8 fixed points



Using 8 corners from Ref and Test image as fixed points

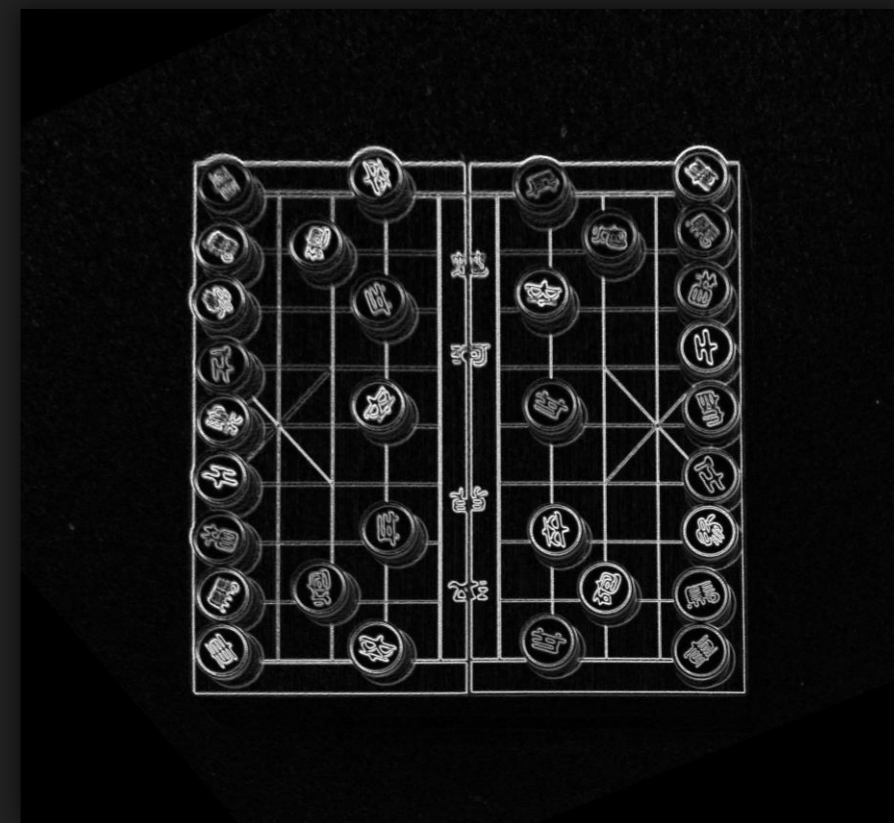
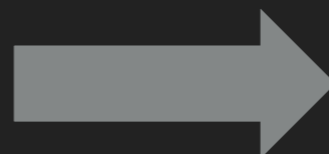
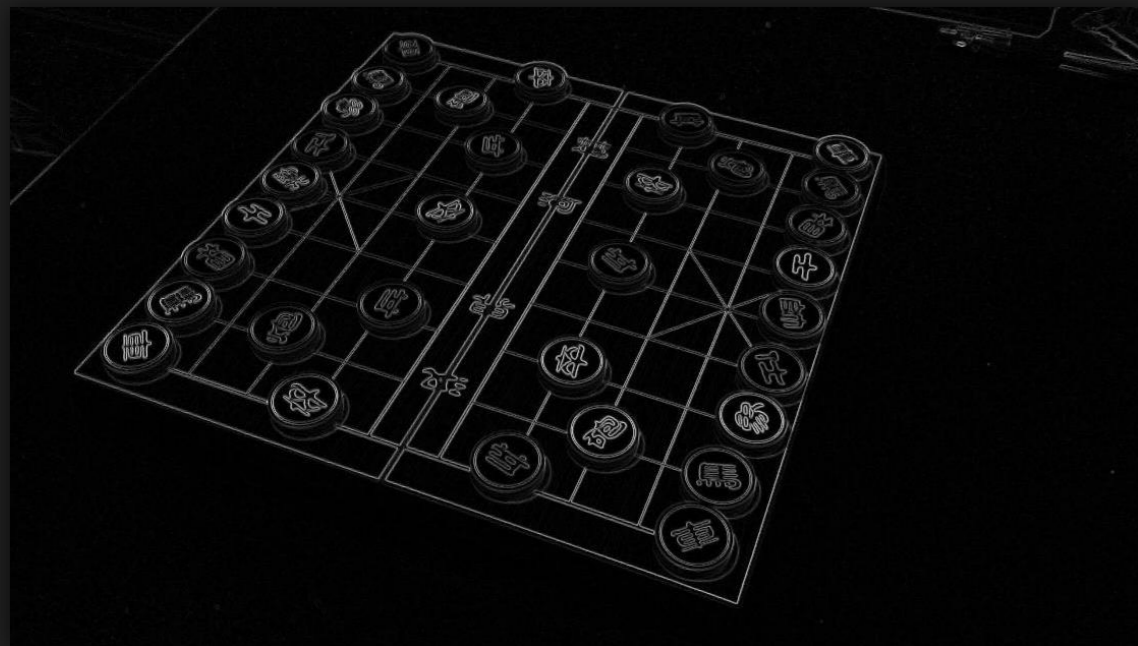
| | | | | | | | | | |
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Transform a leaning image into a straight one

STEP.2 PERSPECTIVE TRANSFORMATION

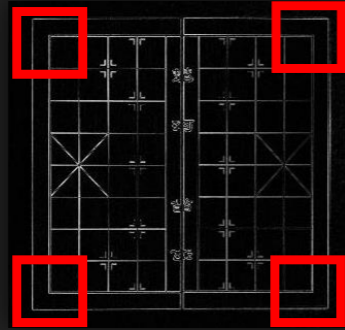
$$(x' \ y' \ w') = (u \ v \ w) \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix}$$

$$x = \frac{x'}{w'}, \quad y = \frac{y'}{w'}.$$



STEP.2 PERSPECTIVE TRANSFORMATION

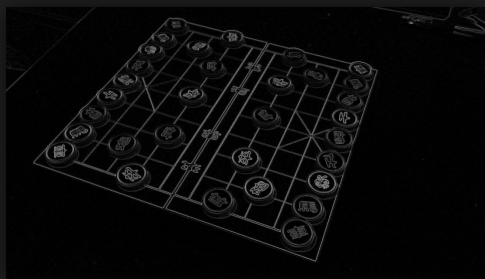
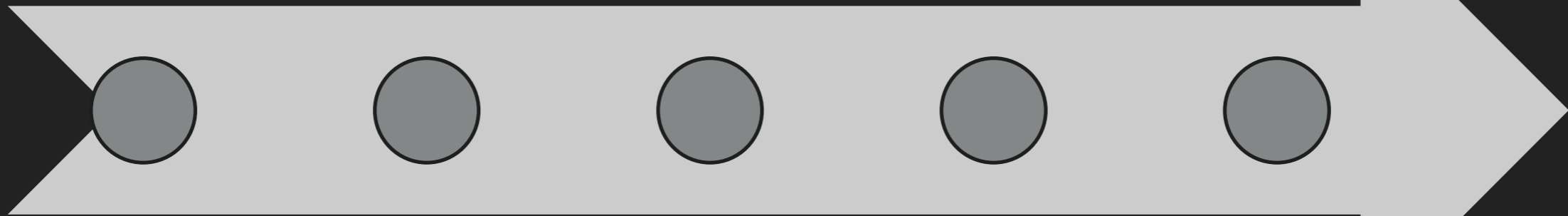
Auto-locate the 4 corners of test image



Calculate transform matrix with the 8 fixed points



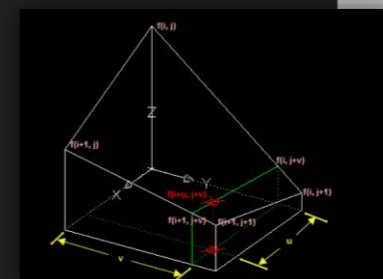
Bilinear interpolation



Using 8 corners from Ref and Test image as fixed points

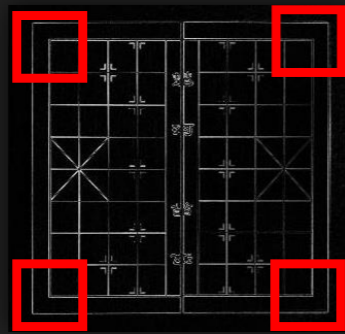
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| 29 | 58 | 57 | 56 | 55 | 54 | 53 | 52 | 51 | 18 |
| 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 |

Transform a leaning image into a straight one

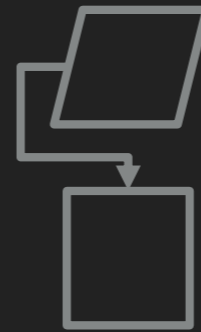


STEP.2 PERSPECTIVE TRANSFORMATION

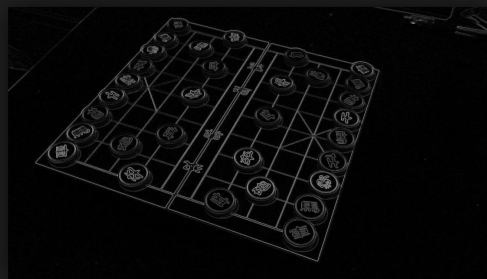
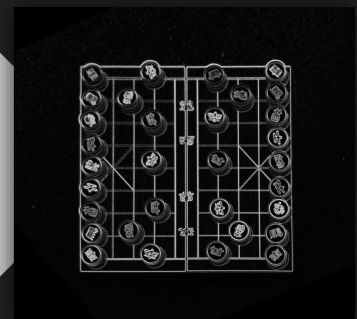
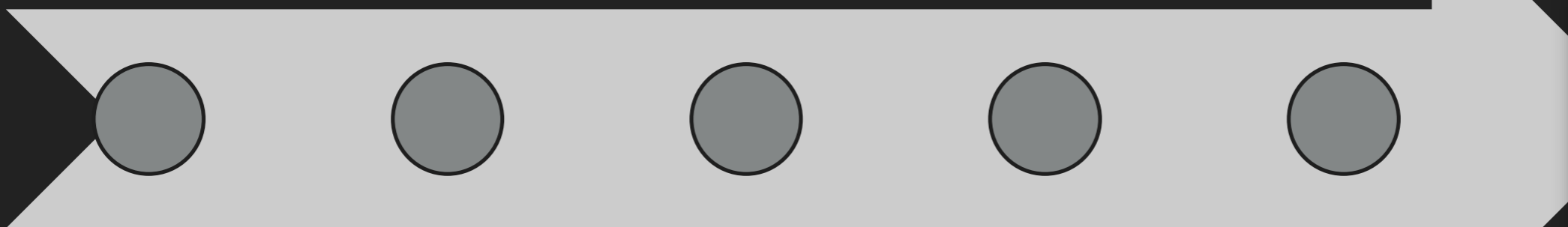
Auto-locate the 4 corners of test image



Calculate transform matrix with the 8 fixed points



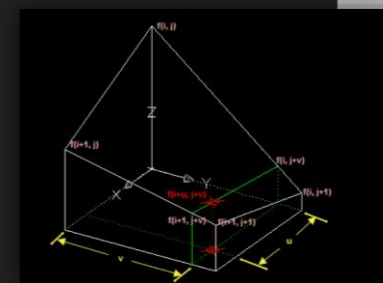
Bilinear interpolation



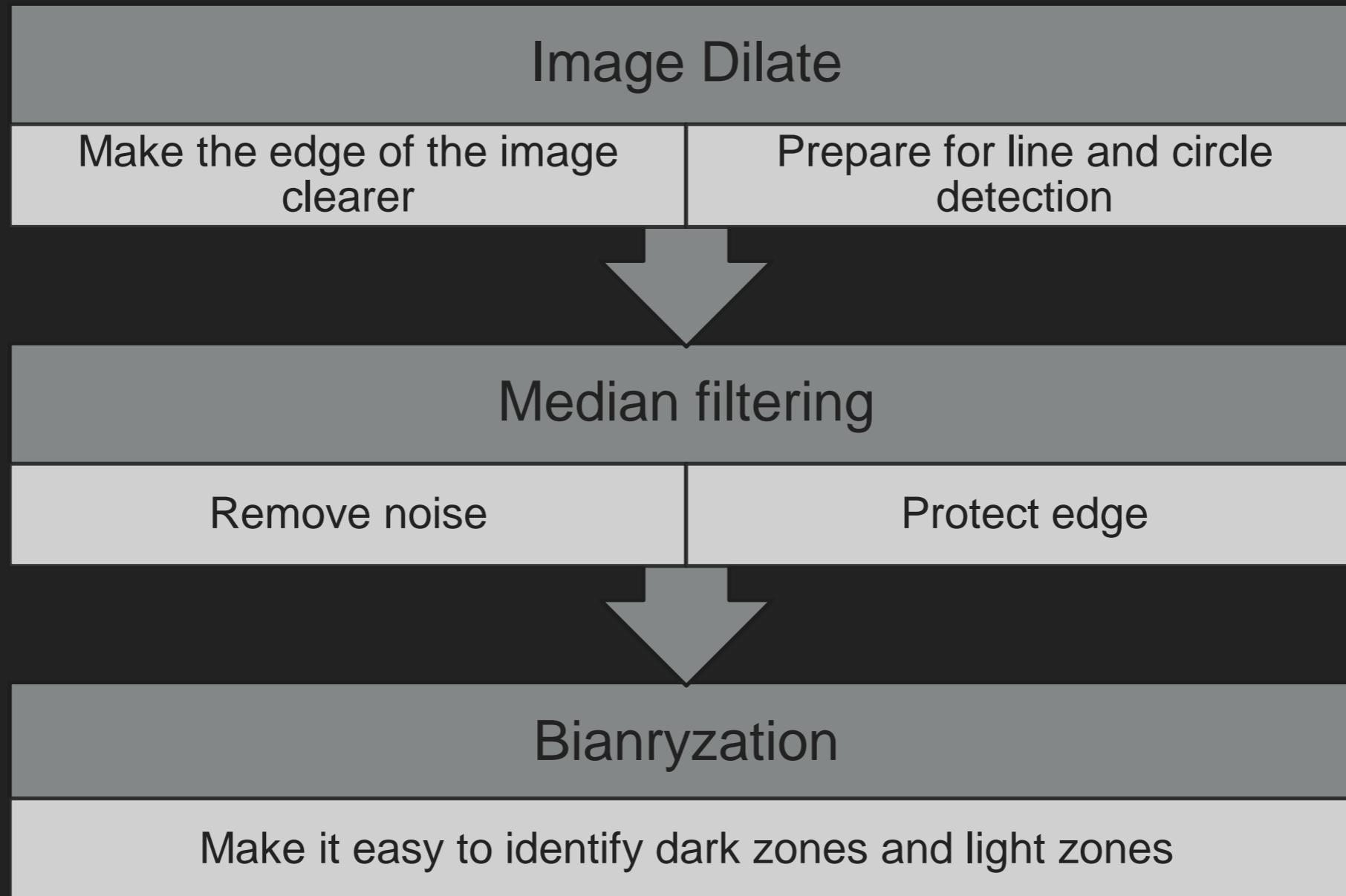
Using 8 corners from Ref and Test image as fixed points

| | | | | | | | | | |
|----|----|----|----|-----|----|----|----|----|----|
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Transform a leaning image into a straight one

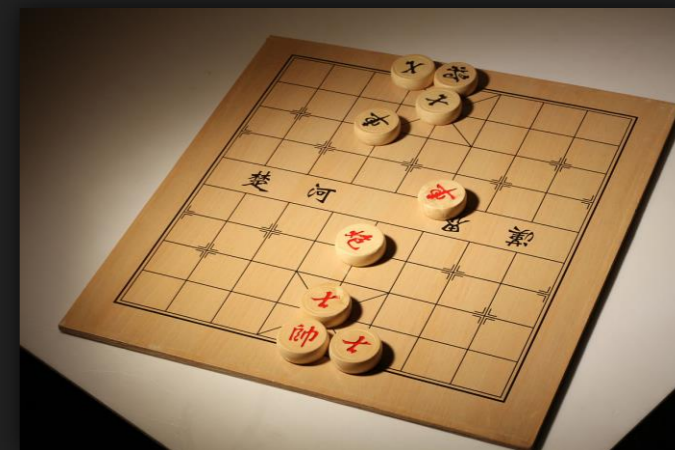
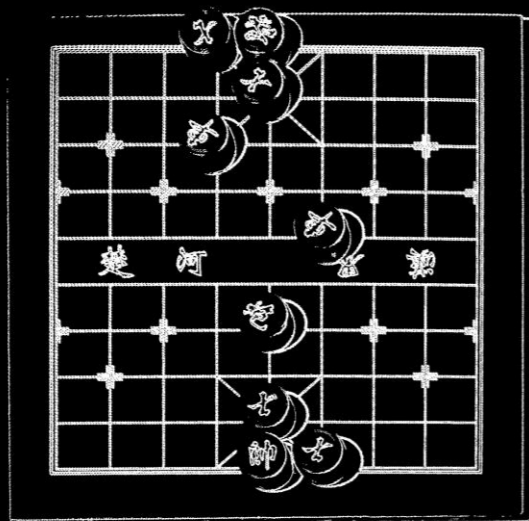


STEP.3 IMAGE QUALITY OPTIMIZE

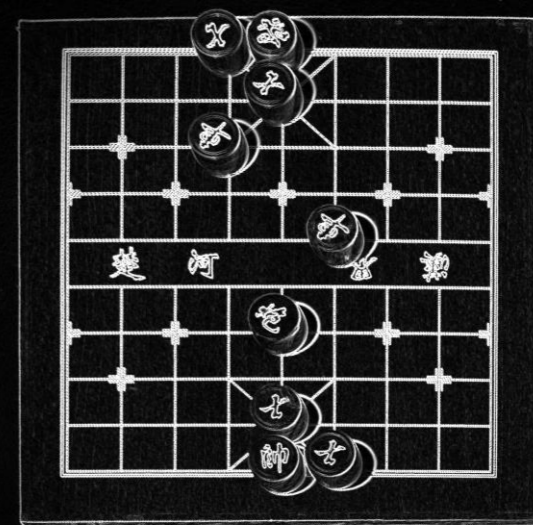


STEP.3 IMAGE QUALITY OPTIMIZE

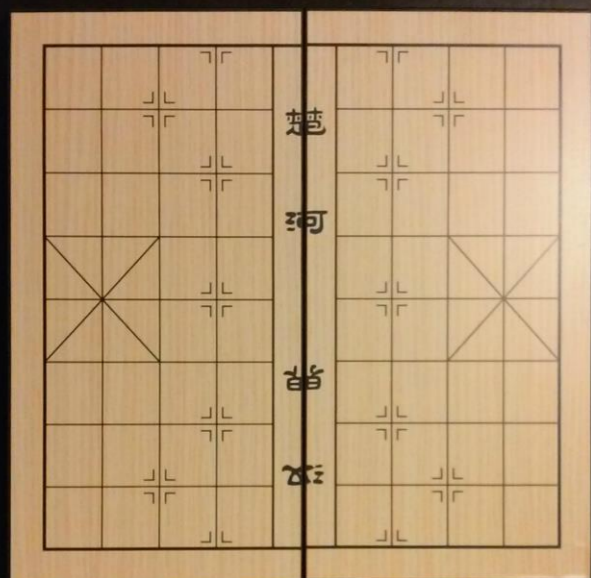
Before optimizing



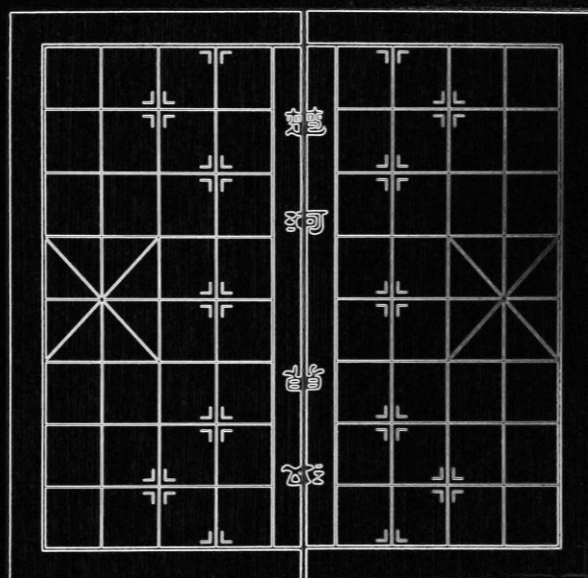
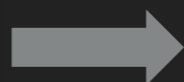
After optimizing



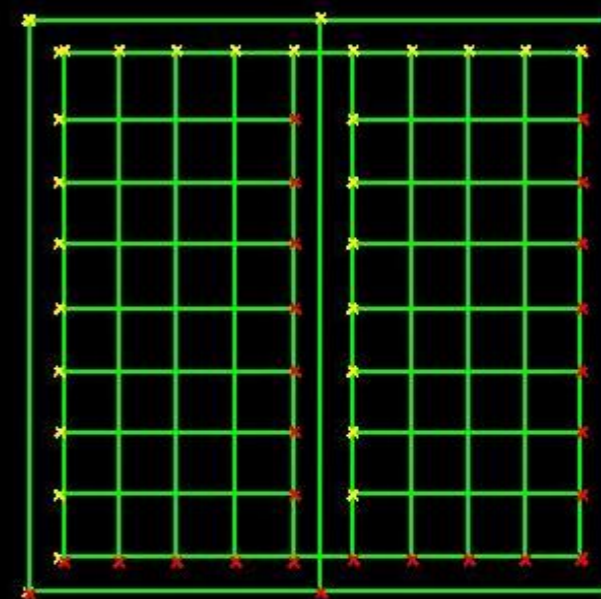
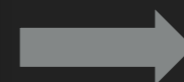
STEP.4 LINE DETECTION



Original



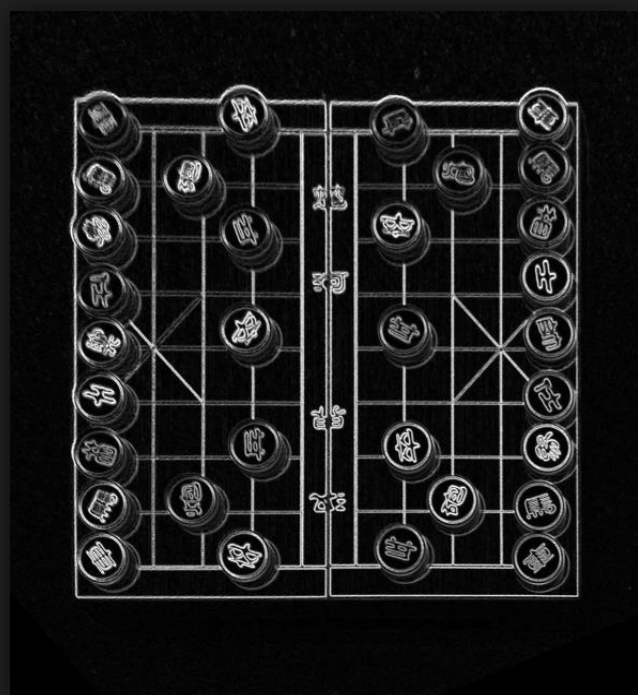
Extract lines



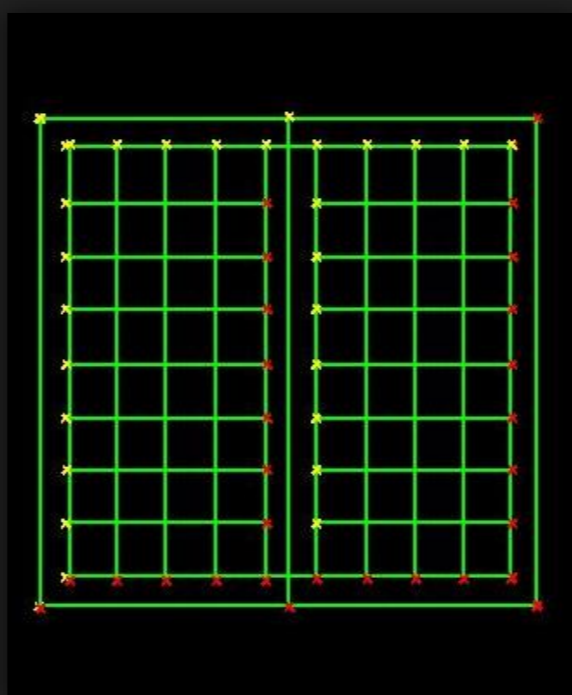
10x9 coordinate

Detecting lines makes it possible to build a “Chess Board Coordinate” !

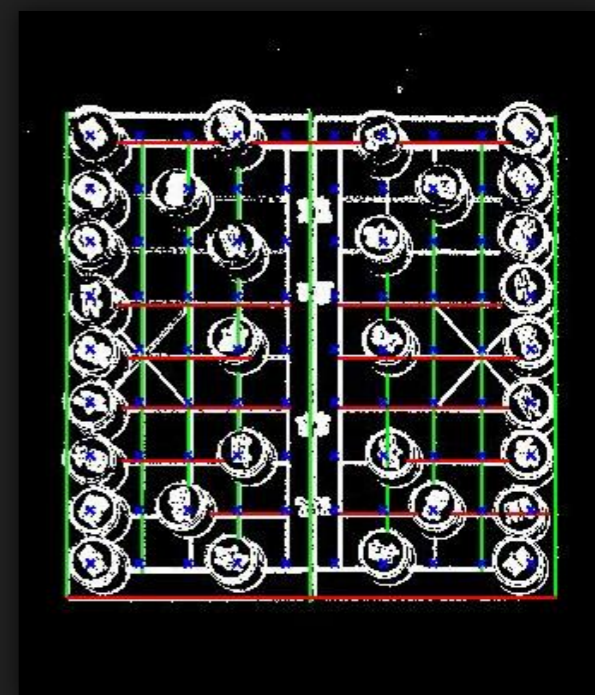
STEP.4 LINE DETECTION



+

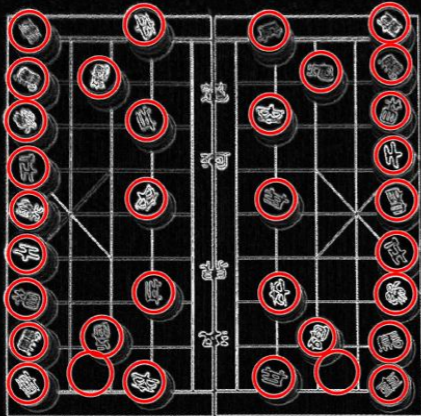


=

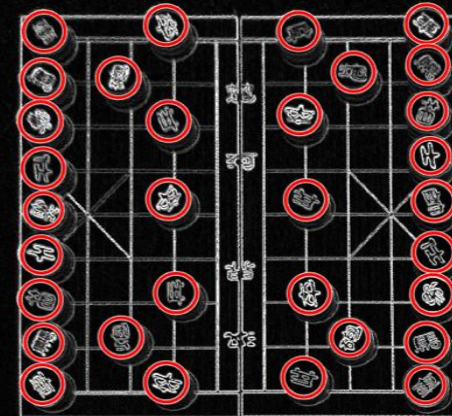


STEP.5 POSITION CHESS PIECES

Find all circles

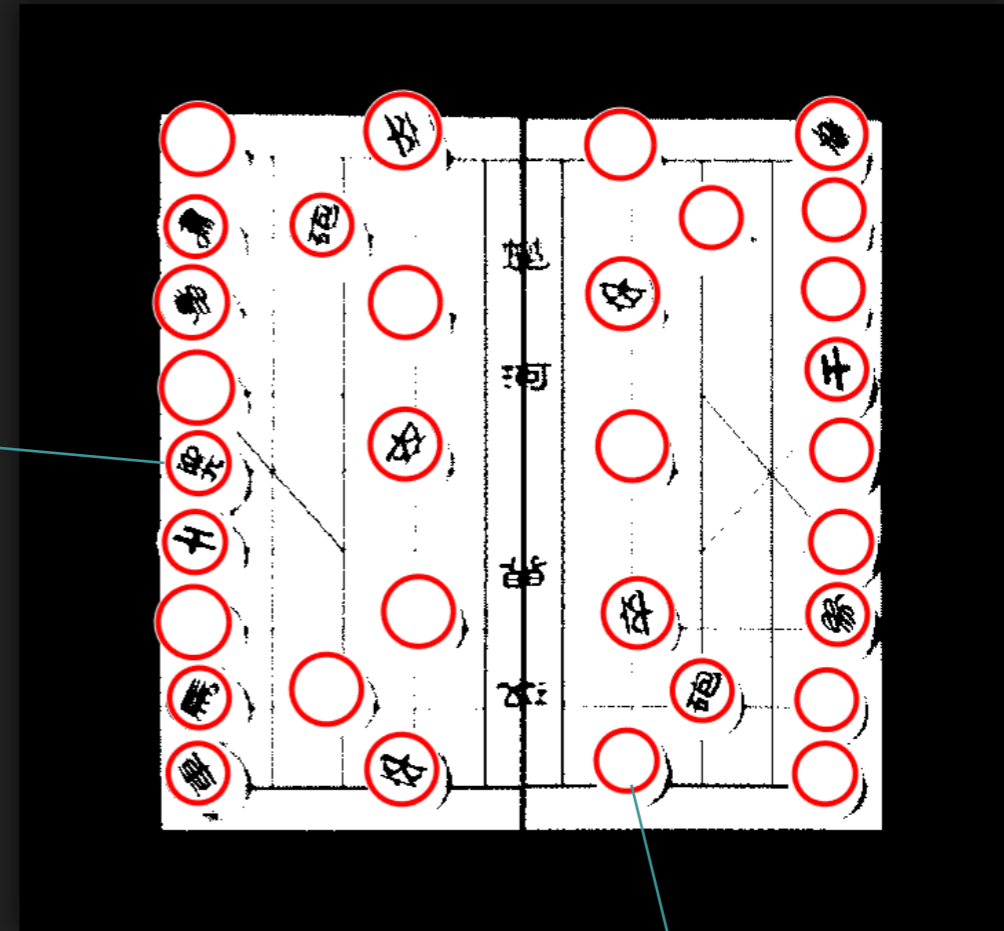
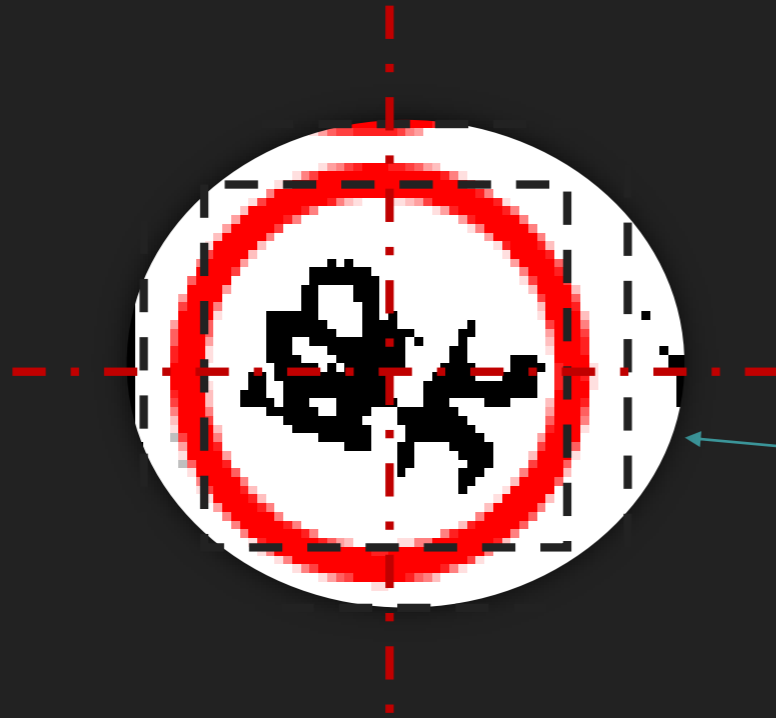


Remove fake circles



```
for i=1:10
  for j=1:9
    for p=1:m
      if((centers(p,1)<point(i,j,1)+min_lines/4)&&(centers(p,1)>point(i,j,1)-min_lines/2.5))
        if((centers(p,2)<point(i,j,2)+min_columns/4)&&(centers(p,2)>point(i,j,2)-min_columns/2.5))
          h = viscircles(centers(p,:),radii(p,:));
          s=sprintf('%d,%d',i,j);
          disp(s);
          break;
        end
      end
    end
  end
end
end
```

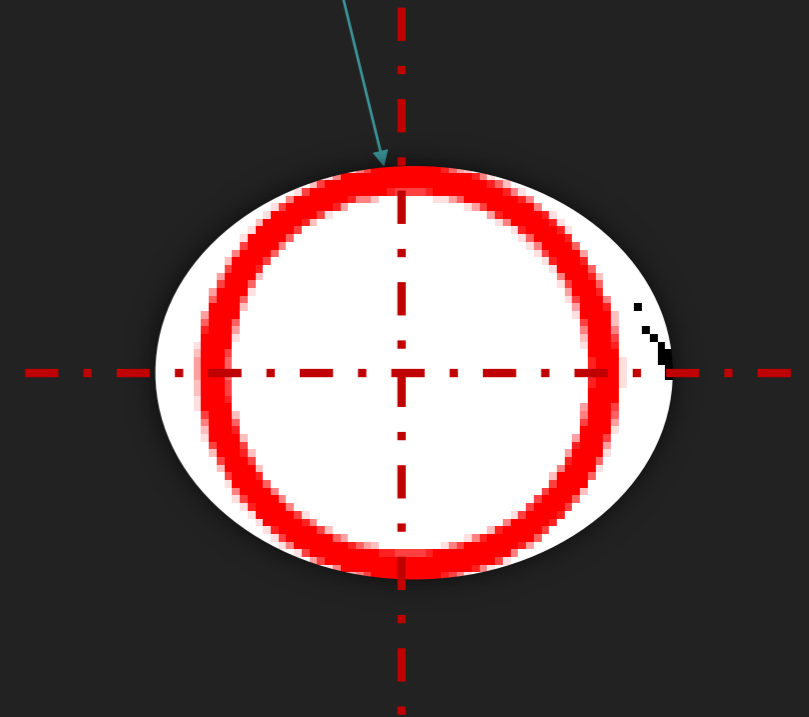
STEP.6 IDENTIFY CHESS PIECES' COLORS



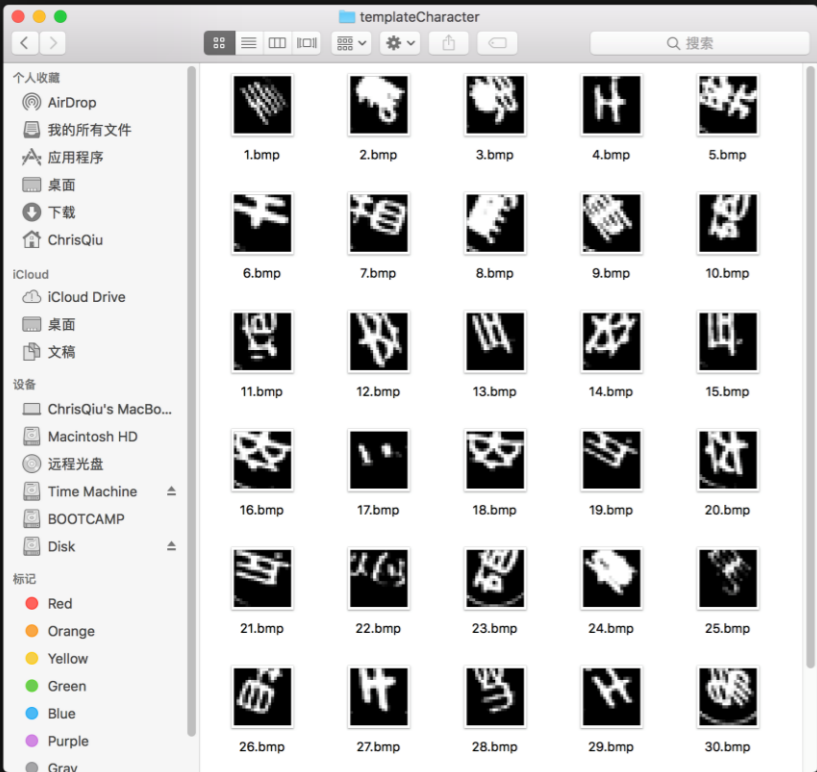
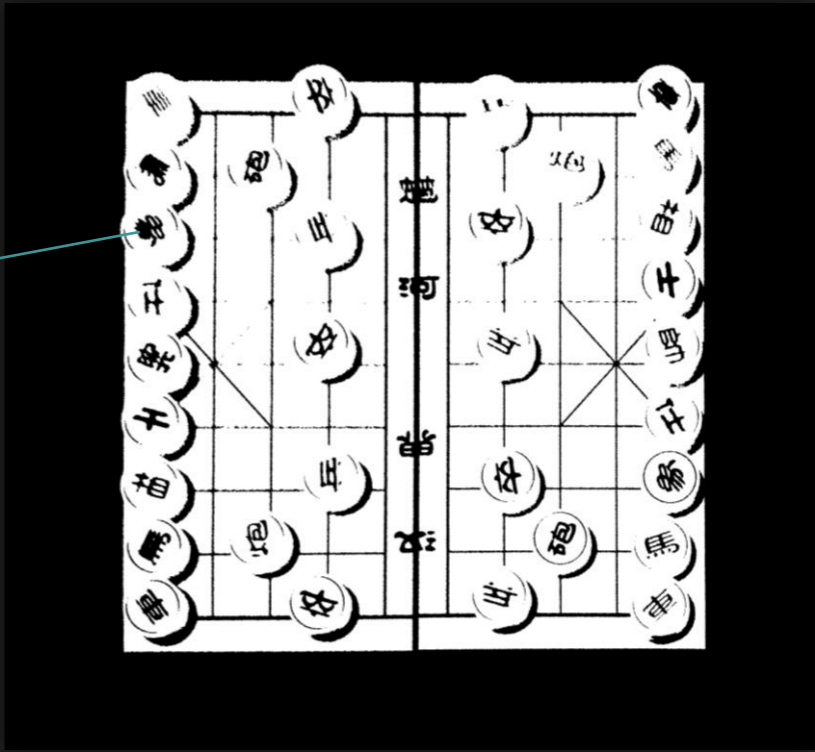
Assuming center coordinate of circle is (x, y) and its radius is r .

$$Pixels = \sum_{t=-\frac{r}{2}}^{\frac{r}{2}} P_{(x,y+t)}$$

If $Pixels > r - pixels$, we consider this chess piece is black.



STEP.7 IDENTIFY CHESS PIECES' CHARACTERS



$$Y_i = \frac{V_i}{\frac{W_i}{T_i} \times \frac{X_i}{U} \sqrt{\frac{(T_i - TUV_i)^2 + (U - TUV_i)^2 + (V_i - TUV_i)^2}{2}}}$$

$$TUV = \frac{T + U + V}{3}$$

PERSONNEL ALLOCATION



张凌霄

- 编写边缘提取、透视变换、直线检测、圆形识别等部分程序
- 安排项目进度



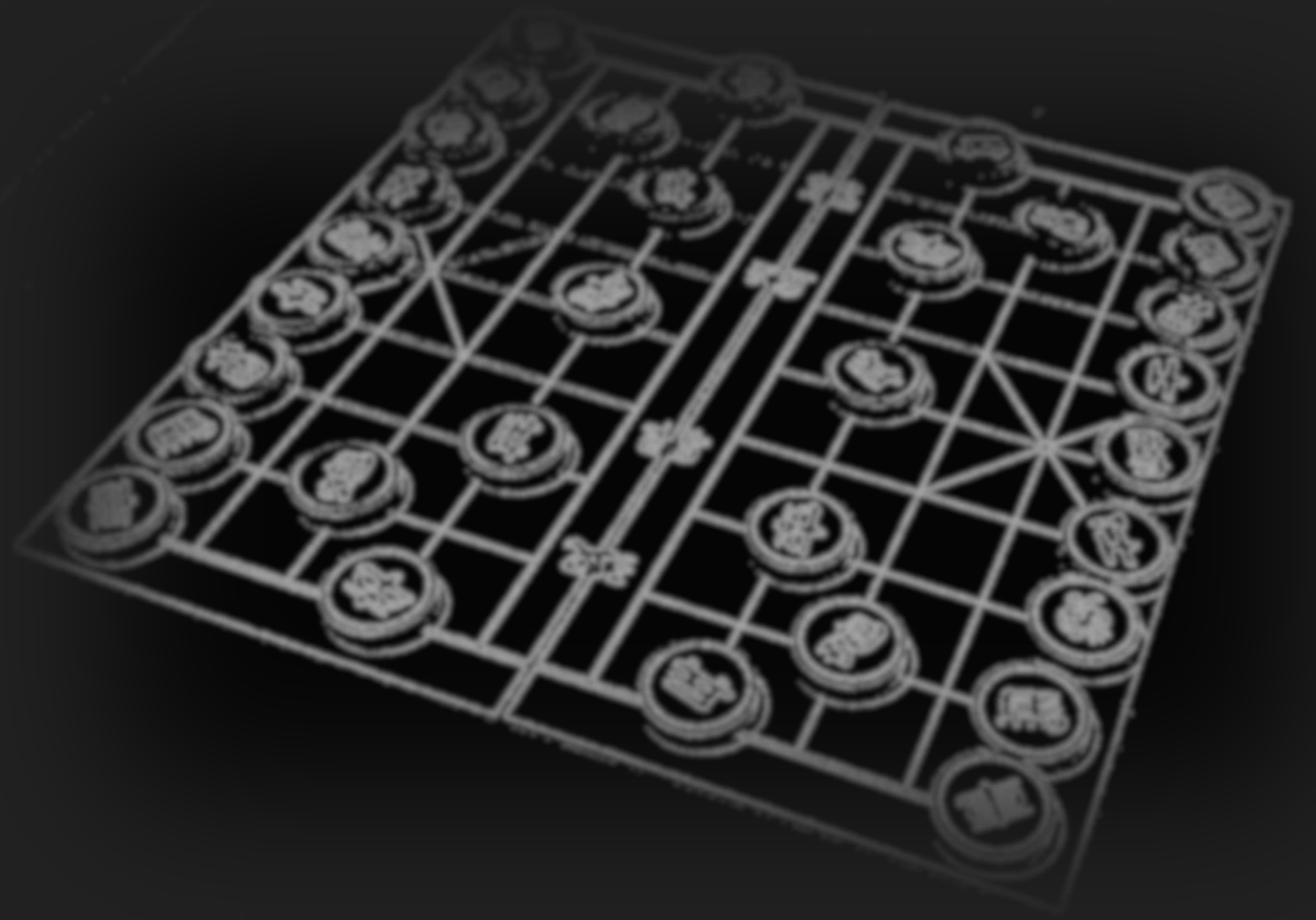
邱子濛

- 编写棋子颜色识别、棋子字符识别等部分程序，建立棋子字符模板
- 制作PPT并展示



郑睦炜

- 编写图像优化部分程序
- 撰写小组报告



基于MATLAB的

象棋棋盘及棋子识别

张凌霄 邱子濛 郑睦炜